

ANALYTICAL AND EXPERIMENTAL INVESTIGATION  
OF PUMPED SOLAR HOT WATER SYSTEMS

BY

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#### ABSTRACT

A transient computer model of a forced circulation solar hot water system has been developed. The model allows for capacitance effects by solving the energy balances on a four node model of the solar collector. The tank model is designed to include the presence of an auxiliary heater and to allow for the nonideal condition of load drawoff.

Five tests were done to validate the computer model. These tests include a comparison of the computer simulation with experimental data and a model available in the literature. The results of these tests indicate that the computer model is able to predict the collector inlet and outlet temperatures within 10% for typical operating conditions.

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REAL TIME (HRS)	LOAD FLOW (GAL)	MASS FLOW (GPH)	COLLECTOR INLET (°F)	COLLECTOR OUTLET (°F)	TEMP. RISE (°F)	TANK 1 (°F)	TANK 2 (°F)	TANK 3 (°F)	TANK 4 (°F)	MEAN TANK (°F)	INSULATION (BTU)	USEFUL GAIN (BTU)	COLLECTOR EFFICIENCY (%)
200.	0.0	58.0	114.6	128.4	13.6	123.2	124.0	120.0	115.7	120.7	1446.7	831.0	57.4
208.	0.0	58.0	115.7	125.4	11.7	123.2	124.7	120.9	116.7	121.4	1036.0	716.7	69.2
215.	0.0	58.0	116.7	120.4	10.7	123.2	125.1	121.7	117.7	121.9	1228.4	652.3	53.1
223.	0.2	58.0	117.7	130.0	12.0	123.2	125.9	122.7	118.6	122.6	1324.6	729.7	55.1
230.	0.2	58.0	118.6	132.6	13.1	123.2	127.1	123.3	119.3	123.2	1502.2	801.4	53.3
238.	0.0	58.0	119.3	131.8	13.3	123.2	128.2	124.3	120.1	124.0	1350.5	810.0	60.0
245.	0.0	58.0	120.1	133.9	13.1	123.1	129.2	125.2	121.2	124.7	1461.5	801.6	54.8
253.	0.1	58.0	121.2	134.7	13.6	123.1	130.3	126.3	122.1	125.5	1457.8	831.6	57.0
300.	0.2	58.0	122.1	133.7	12.5	123.2	131.2	127.2	122.9	126.1	1254.3	765.5	61.0
308.	0.0	58.0	122.9	136.2	12.4	123.2	131.9	128.1	123.8	126.7	1417.1	758.7	53.5
315.	0.0	58.0	123.8	135.3	12.4	123.2	132.8	129.1	124.8	127.5	1254.3	757.2	60.4
323.	0.0	58.0	124.8	135.8	11.2	123.1	133.4	129.8	125.9	128.1	1198.8	684.8	57.1
330.	0.1	58.0	125.9	135.8	10.4	123.1	133.8	130.7	126.8	128.6	1117.4	636.0	56.9
338.	0.1	58.0	126.8	139.0	11.1	123.2	134.6	131.4	127.5	129.2	1365.3	675.1	49.4
345.	0.1	58.0	127.5	137.2	10.9	123.2	135.4	132.3	128.3	129.8	1117.4	666.5	59.6
353.	0.1	58.0	128.3	138.1	9.7	123.2	135.9	132.8	129.1	130.2	1117.4	593.7	53.1
400.	0.2	58.0	129.1	138.6	9.7	123.3	136.3	133.6	129.8	130.7	1106.3	588.8	53.2









































































































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1 REAL K,MF
2 DIMENSION RAD(90),TAMB(90),TINL(90)
3 DATA PI/3.14159/
4 READ, LL
5 READ,WT,D,K,DEL,HF,SIG,EP,EG,DEP,PER,A,TAUA
6 IFLAG=0
7 MF=488.
8 WS=2.
9 WRITE(6,91)
10 91 FORMAT('1'////)
11 READ,(RAD(I),I=1,LL)
12 READ,(TAMB(I),I=1,LL)
13 READ,(TINL(I),I=1,LL)
14 DO 100 L=1,LL
15 S=RAD(L)*8.
16 TA=TAMB(L)+460.
17 TIN=TINL(L)+460.
18 SS=S
19 S=S*TAUA
20 IF(IFLAG.EQ.0) TM=TA*30.
21 IF(IFLAG.EQ.0) TG=TA*15.
22 5 HRPG=(SIG*(TM*TM+TG*TG)*(TM+TG))/(1./EP+1./EG-1.)
23 HCPG=.21*(TM-TG)*.25
24 HRGA=SIG*EG*(TG*TG+TA*TA)*(TG+TA)
25 HW=1.*.3*WS
26 TGC=(TM*(HRPG+HCPG)+TA*(HRGA+HW))/(HRGA+HW+HCPG+HRPG)
27 ERR=ABS(TGC-TG)
28 IF(ERR.LT.1.) GO TO 10
29 TG=TG+.5*(TGC-TG)
30 GO TO 5
31 10 TG=TGC
32 QTOP=HRGA*(TG-TA)+HW*(TG-TA)
33 QBOT=.1*QTOP
34 QEDGE=.08*DEP*PER*(TM-TA)/A
35 QTOT=QTOP+QBOT+QEDGE
36 UL=QTOT/(TM-TA)
37 PART=((UL/(K*DEL))**.5*(WT-D)/2.)
38 F=TANH(PART)/PART
39 FPP=F*(WT-D)/WT + D/WT
40 FP=FPP/(1.+FPP*UL*WT/(HF*PI*D))
41 FR=(MF/(A*UL))*(1.-EXP(-FP*UL*A/MF))
42 QU=FR*(S-UL*(TIN-TA))*A
43 TMC=TIN+(QU/(A*UL))*(1./FR-1./FP)
44 ERR1=ABS(TMC-TM)
45 IF (ERR1 .LE. 1.) GO TO 30
46 TM=TM+.2*(TMC-TM)
47 GO TO 5
48 30 TOUT=QU/MF+TIN
49 TM=TMC
50 SS=SS*A
51 EFF=(QU/SS)*100.
52 TA=TA-460.
53 TMC=TMC-460.
54 TGC=TGC-460.
55 TIN=TIN-460.
56 TOUT=TOUT-460.
57 TRISE=TOUT-TIN
58 QU=QU/8.
59 SS=SS/8.
60 WRITE(6,90) MF,TMC,TGC,UL,FP,FR,TA,TIN,TOUT,TRISE,SS,QU,EFF
61 90 FORMAT('1',F10.1,2F9.1,3F9.2,7F9.1)
62 IFLAG=1
63 100 CONTINUE
64 STOP
65 END

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